

# Chapter Ten

## WAVE OPTICS



### MCQ I

**10.1** Consider a light beam incident from air to a glass slab at Brewster's angle as shown in Fig. 10.1.

A polaroid is placed in the path of the emergent ray at point P and rotated about an axis passing through the centre and perpendicular to the plane of the polaroid.

- (a) For a particular orientation there shall be darkness as observed through the polaroid.
- (b) The intensity of light as seen through the polaroid shall be independent of the rotation.
- (c) The intensity of light as seen through the Polaroid shall go through a minimum but not zero for two orientations of the polaroid.
- (d) The intensity of light as seen through the polaroid shall go through a minimum for four orientations of the polaroid.

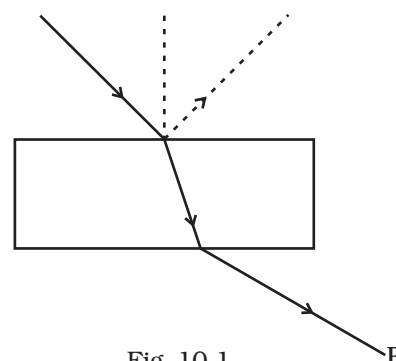


Fig. 10.1

**10.2** Consider sunlight incident on a slit of width  $10^4 \text{ \AA}$ . The image seen through the slit shall



- (a) be a fine sharp slit white in colour at the center.
- (b) a bright slit white at the center diffusing to zero intensities at the edges.
- (c) a bright slit white at the center diffusing to regions of different colours.
- (d) only be a diffused slit white in colour.

**10.3** Consider a ray of light incident from air onto a slab of glass (refractive index  $n$ ) of width  $d$ , at an angle  $\theta$ . The phase difference between the ray reflected by the top surface of the glass and the bottom surface is

- (a)  $\frac{4\pi d}{\lambda} \left(1 - \frac{1}{n^2} \sin^2 \theta\right)^{1/2} + \pi$
- (b)  $\frac{4\pi d}{\lambda} \left(1 - \frac{1}{n^2} \sin^2 \theta\right)^{1/2}$
- (c)  $\frac{4\pi d}{\lambda} \left(1 - \frac{1}{n^2} \sin^2 \theta\right)^{1/2} + \frac{\pi}{2}$
- (d)  $\frac{4\pi d}{\lambda} \left(1 - \frac{1}{n^2} \sin^2 \theta\right)^{1/2} + 2\pi$

**10.4** In a Young's double slit experiment, the source is white light. One of the holes is covered by a red filter and another by a blue filter. In this case

- (a) there shall be alternate interference patterns of red and blue.
- (b) there shall be an interference pattern for red distinct from that for blue.
- (c) there shall be no interference fringes.
- (d) there shall be an interference pattern for red mixing with one for blue.

**10.5** Figure 10.2 shows a standard two slit arrangement with slits  $S_1, S_2$ .  $P_1, P_2$  are the two minima points on either side of  $P$  (Fig. 10.2).

At  $P_2$  on the screen, there is a hole and behind  $P_2$  is a second 2-slit arrangement with slits  $S_3, S_4$  and a second screen behind them.

- (a) There would be no interference pattern on the second screen but it would be lighted.
- (b) The second screen would be totally dark.

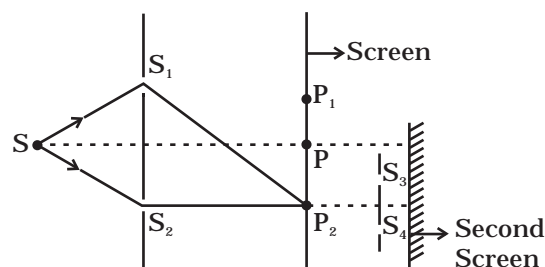
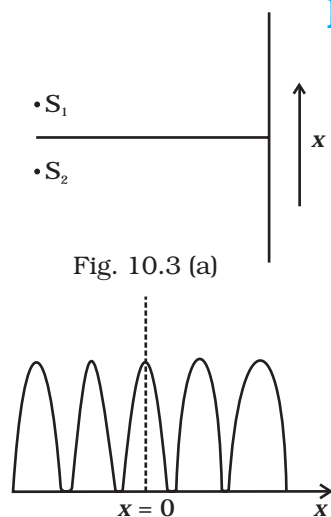


Fig. 10.2

- (c) There would be a single bright point on the second screen.  
 (d) There would be a regular two slit pattern on the second screen.

## MCQ II



**10.6** Two sources  $S_1$  and  $S_2$  of intensities  $I_1$  and  $I_2$  are placed in front of a screen [Fig. 10.3 (a)]. The pattern of intensity distribution seen in the central portion is given by Fig. 10.3 (b).

In this case which of the following statements are true.

- (a)  $S_1$  and  $S_2$  have the same intensities.
- (b)  $S_1$  and  $S_2$  have a constant phase difference.
- (c)  $S_1$  and  $S_2$  have the same phase.
- (d)  $S_1$  and  $S_2$  have the same wavelength.

**10.7** Consider sunlight incident on a pinhole of width  $10^3 \text{ \AA}$ . The image of the pinhole seen on a screen shall be

- (a) a sharp white ring.
- (b) different from a geometrical image.
- (c) a diffused central spot, white in colour.
- (d) diffused coloured region around a sharp central white spot.

**10.8** Consider the diffraction pattern for a small pinhole. As the size of the hole is increased

- (a) the size decreases.
- (b) the intensity increases.
- (c) the size increases.
- (d) the intensity decreases.

**10.9** For light diverging from a point source

- (a) the wavefront is spherical.
- (b) the intensity decreases in proportion to the distance squared.
- (c) the wavefront is parabolic.
- (d) the intensity at the wavefront does not depend on the distance.

## VSA

**10.10** Is Huygen's principle valid for longitudinal sound waves?

**10.11** Consider a point at the focal point of a convergent lens. Another convergent lens of short focal length is placed on the other side. What is the nature of the wavefronts emerging from the final image?

**10.12** What is the shape of the wavefront on earth for sunlight?

- 10.13** Why is the diffraction of sound waves more evident in daily experience than that of light wave?
- 10.14** The human eye has an approximate angular resolution of  $\phi = 5.8 \times 10^{-4}$  rad and a typical photocopier prints a minimum of 300 dpi (dots per inch, 1 inch = 2.54 cm). At what minimal distance  $z$  should a printed page be held so that one does not see the individual dots.
- 10.15** A polaroid (I) is placed in front of a monochromatic source. Another polaroid (II) is placed in front of this polaroid (I) and rotated till no light passes. A third polaroid (III) is now placed in between (I) and (II). In this case, will light emerge from (II). Explain.

## SA

- 10.16** Can reflection result in plane polarised light if the light is incident on the interface from the side with higher refractive index?
- 10.17** For the same objective, find the ratio of the least separation between two points to be distinguished by a microscope for light of  $5000 \text{ \AA}$  and electrons accelerated through 100V used as the illuminating substance.
- 10.18** Consider a two slit interference arrangements (Fig. 10.4) such that the distance of the screen from the slits is half the distance between the slits. Obtain the value of  $D$  in terms of  $\lambda$  such that the first minima on the screen falls at a distance  $D$  from the centre O.

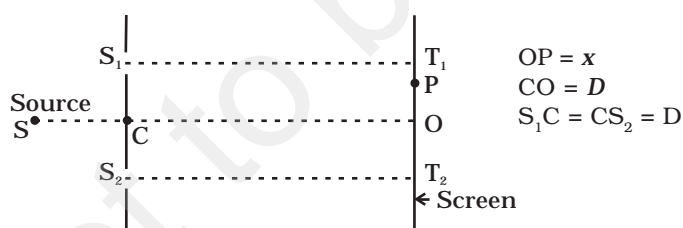


Fig. 10.4

## LA

- 10.19** Figure 10.5 shown a two slit arrangement with a source which emits unpolarised light. P is a polariser with axis whose direction is not given. If  $I_0$  is the intensity of the principal maxima when *no* polariser is present, calculate in the present case, the intensity of the principal maxima as well as of the first minima.

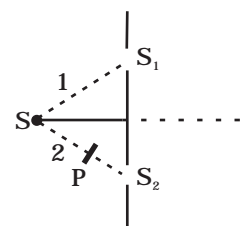


Fig. 10.5

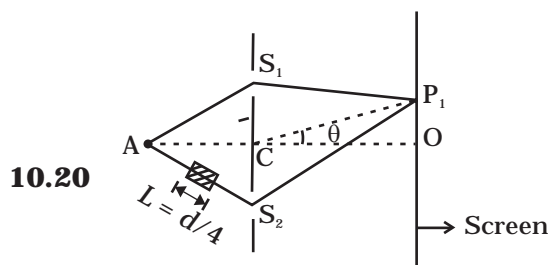


Fig. 10.6

$$AC = CO = D, S_1C = S_2C = d \ll D$$

A small transparent slab containing material of  $\mu = 1.5$  is placed along  $AS_2$  (Fig. 10.6). What will be the distance from O of the principal maxima and of the first minima on either side of the principal maxima obtained in the absence of the glass slab. .

**10.21** Four identical monochromatic sources A,B,C,D as shown in the (Fig. 10.7) produce waves of the same wavelength  $\lambda$  and are coherent. Two receiver  $R_1$  and  $R_2$  are at great but equal distances from B.

- Which of the two receivers picks up the larger signal?
- Which of the two receivers picks up the larger signal when B is turned off?
- Which of the two receivers picks up the larger signal when D is turned off?
- Which of the two receivers can distinguish which of the sources B or D has been turned off?

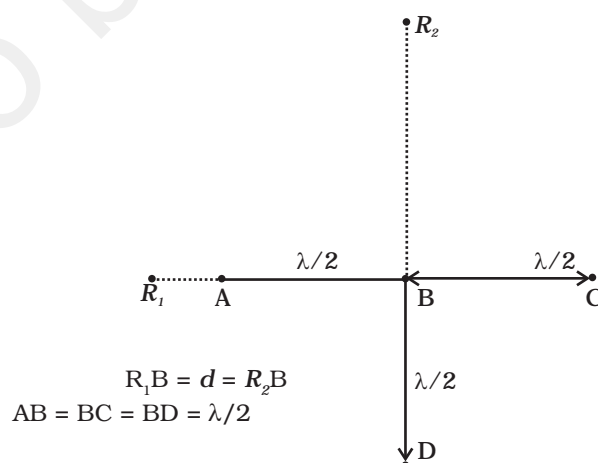


Fig. 10.7

**10.22** The optical properties of a medium are governed by the relative permittivity ( $\epsilon_r$ ) and relative permeability ( $\mu_r$ ). The refractive index is defined as  $\sqrt{\mu_r \epsilon_r} = n$ . For ordinary material  $\epsilon_r > 0$  and  $\mu_r > 0$  and the positive sign is taken for the square root. In 1964, a Russian scientist V. Veselago postulated the existence of material with  $\epsilon_r < 0$  and  $\mu_r < 0$ . Since then such 'metamaterials' have been produced in the laboratories and their optical properties studied. For such materials  $n = -\sqrt{\mu_r \epsilon_r}$ . As light enters a medium of such refractive index the phases travel away from the direction of propagation.

- (i) According to the description above show that if rays of light enter such a medium from air (refractive index = 1) at an angle  $\theta$  in 2<sup>nd</sup> quadrant, then the refracted beam is in the 3<sup>rd</sup> quadrant.
- (ii) Prove that Snell's law holds for such a medium.

**10.23** To ensure almost 100 per cent transmittivity, photographic lenses are often coated with a thin layer of dielectric material. The refractive index of this material is intermediated between that of air and glass (which makes the optical element of the lens). A typically used dielectric film is  $\text{MgF}_2$  ( $n = 1.38$ ). What should the thickness of the film be so that at the center of the visible spectrum ( $5500 \text{ \AA}$ ) there is maximum transmission.

